

When a square root, or cube, or any other root, of a number can't be shown as a whole number or fraction, we call this a surd.

For example, the square of five, or 12, or 20. Non-surds would be perfect squares.

Like the square root of four is two and the square root of 100 is 10.

Surds can be multiplied using the rule $\sqrt{A} \times \sqrt{B} = \sqrt{AB}$.

For example, $\sqrt{3} \times \sqrt{4}$, equals $\sqrt{3 \times 4}$, which is $\sqrt{12}$.

Surds can also be divided. The rule is $\frac{\sqrt{A}}{\sqrt{B}} = \sqrt{\frac{A}{B}}$.

$\frac{\sqrt{64}}{\sqrt{16}}$, becomes $\sqrt{\frac{64}{16}}$.

Which can be simplified as $\sqrt{4}$, which is two.

Notice that $\sqrt{A} \times \sqrt{A} = A$.

So, $\sqrt{3} \times \sqrt{3} = \sqrt{9}$. And the square root of nine is three.

You might be asked to simplify a surd, for example $\sqrt{45}$. To do this you need to check if any factors of 45 are perfect squares. The Factor pairs of 45 are one and 45, three and 15 and five and nine. The factor pair to use is five and nine, as nine is a square number, so we can write $\sqrt{45}$ as $\sqrt{9 \times 5}$.

The square root of nine is three, so we can write this as three times $\sqrt{5}$.

That's our surd simplified.

The rules of surds make it possible to simplify complex calculations exactly.